

## Discovery of Bimodal Drift Rate Structure in FRB 20240114A: Evidence for Dual Emission Regions

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### 4 ABSTRACT

5 We report the discovery of bimodal structure in the drift rate distribution of upward-drifting burst  
6 clusters from the hyperactive repeating fast radio burst FRB 20240114A. Using unsupervised machine  
7 learning (HDBSCAN density-based clustering applied directly to an 8-dimensional standardized feature  
8 space, with UMAP used only for post-hoc visualization) applied to 233 upward-drifting burst clusters  
9 from the FAST telescope dataset, we identify a distinct subpopulation of 45 burst clusters (hereafter  
10 Cluster C1) with **mean** drift rates 2.5× higher than typical upward-drifting burst clusters (245.6 vs  
11 98.1 MHz/ms). Gaussian mixture modeling reveals strong evidence for bimodality ( $\Delta\text{BIC} = 296.6$ ),  
12 with clearly separated modes (Ashman’s  $D = 2.70 > 2$ ; Ashman et al. 1994) and a statistically significant  
13 gap in the distribution ( $11.3\sigma$ ). **Crucially, all 45 C1 members are single-component (U1)**  
14 **burst clusters with drift rates well above their measurement uncertainties (minimum**  
15 **87.1 MHz/ms, typical error  $\sim 3\text{--}65$  MHz/ms).** Crucially, we demonstrate that this bimodality  
16 persists when restricting the analysis to single-component (U1) burst clusters only ( $n = 142$ ; **none**  
17 **consistent with zero drift within errors):**  $\Delta\text{BIC} = 19.9$ , Ashman’s  $D = 2.71$ , gap significance  
18  $= 9.2\sigma$ , confirming that the result is not an artifact of combining single- and multi-component burst  
19 clusters with different drift rate definitions **nor of measurement-error contamination near the**  
20 **drift-rate floor.** The extreme-drift subpopulation also exhibits systematically lower peak frequencies  
21 ( $-7\%$ ), shorter durations ( $-29\%$ ), and distinct clustering in multi-dimensional feature space. **These**  
22 **findings are suggestive of two spatially separated emission regions in the magnetosphere,**  
23 **each producing upward-drifting burst clusters with distinct physical characteristics, al-**  
24 **though confirmation requires observations from additional epochs and sources.**

25 *Keywords:* Fast radio bursts — Magnetars — Radio transient sources — Machine learning

### 26 1. INTRODUCTION

27 Fast radio bursts (FRBs) are millisecond-duration ra-  
28 dio transients of extragalactic origin (Lorimer et al.  
29 2007; Thornton et al. 2013), whose physical mechanism  
30 remains debated (Petroff et al. 2022). The discovery  
31 of repeating FRBs (Spitler et al. 2016) has enabled de-  
32 tailed morphological studies of individual sources, re-  
33 vealing complex time-frequency structure including sub-  
34 burst drift rates (Hessels et al. 2019), spectro-temporal  
35 correlations (Rajabi et al. 2020; Chamma et al. 2023),  
36 and diverse morphological classes (Pleunis et al. 2021;  
37 CHIME/FRB Collaboration 2021).

38 FRB 20240114A, discovered in January 2024, ex-  
39 hibits an exceptionally high burst rate, making it an  
40 ideal laboratory for statistical studies of burst prop-  
41 erties. Recent work by Zhang et al. (2026) classified  
42 978 drifting burst clusters from FRB 20240114A into  
43 upward-drifting (23.8%) and downward-drifting (76.2%)  
44 populations based on their sub-burst drift rates, us-  
45 ing data obtained with the Five-hundred-meter Aper-  
46 ture Spherical Telescope (FAST). They further clas-  
47 sified burst clusters by internal morphology: single-  
48 component (U1/D1), double-component (U2/D2), and  
49 multi-component (Um/Dm), where the drift rate def-  
50 inition differs between these categories—for single-  
51 component burst clusters it characterizes the intrin-  
52 sic frequency-time evolution, while for **double/multi-**  
53 **component** burst clusters it reflects the relative sepa-  
54 ration between sub-bursts.

55 Their analysis found systematic differences be-  
 56 tween upward- and downward-drifting popula-  
 57 tions (defined using consecutive time intervals)  
 58 using Kolmogorov-Smirnov tests, though such  
 59 differences do not necessarily hold for burst  
 60 clusters defined with intermittent time intervals  
 61 (Zhang et al. 2026). Each drift-direction class  
 62 was treated as internally homogeneous.

63 In this paper, we apply unsupervised machine learn-  
 64 ing to search for *hidden substructure* within these mor-  
 65 phological classes. We discover that the upward-drifting  
 66 population contains two statistically distinct subpopu-  
 67 lations, and demonstrate that this bimodality persists  
 68 even when restricting to single-component burst clus-  
 69 ters alone, ruling out definitional artifacts.

## 70 2. DATA AND METHODS

### 71 2.1. Dataset

72 We analyze the publicly available FRB 20240114A  
 73 Morphology Dataset (Zhang et al. 2026), containing  
 74 978 burst clusters with measurable drift rates observed  
 75 by FAST on 2024 March 12. For each burst cluster,  
 76 we extract eight physical features: bandwidth, effective  
 77 width, peak frequency, drift rate, energy, flux, signal-to-  
 78 noise ratio, and center frequency. As noted by Zhang  
 79 et al. (2026), the 233 upward-drifting burst clusters  
 80 comprise 142 single-component (U1; 60.9%), 86 double-  
 81 component (U2; 36.9%), and 5 multi-component (Um;  
 82 2.1%) burst clusters.

83 We note that the tabulated features (bandwidth, effec-  
 84 tive width, peak frequency, energy, flux, S/N, and center  
 85 frequency) in the morphology table correspond to a rep-  
 86 resentative burst within each burst cluster, while only  
 87 the first seven columns are defined at the burst cluster  
 88 level (Zhang et al. 2026). Our analysis uses the burst  
 89 cluster-level quantities as provided in the public release.

90 **Drift rate measurement uncertainties are pro-**  
 91 **vided in the public catalogue (Zhang et al. 2026).**  
 92 **Among the 233 upward-drifting burst clusters,**  
 93 **87 have drift rates below 50 MHz/ms; all 87 are**  
 94 **U2 or Um morphology, and 42 of these are con-**  
 95 **sistent with zero within their measurement er-**  
 96 **rors. In contrast, among the 142 U1 burst clus-**  
 97 **ters, zero have drift rates consistent with zero**  
 98 **(minimum drift rate 87.1 MHz/ms; typical er-**  
 99 **rors 3–65 MHz/ms). This distinction between**  
 100 **U1 and U2/Um measurement reliability moti-**  
 101 **vates the U1-only control analysis presented in**  
 102 **Section 3.3.**

### 103 2.2. Unsupervised Clustering

104 **Feature preprocessing.** Each feature is standard-  
 105 ized to zero mean and unit variance, with flux, energy,  
 106 and bandwidth log-transformed first to compress their  
 107 heavy tails.

108 **Density-based clustering.** We apply Hierarchi-  
 109 cal Density-Based Spatial Clustering of Applications  
 110 with Noise (HDBSCAN; Campello et al. 2013) di-  
 111 rectly to the standardized 8-dimensional feature space  
 112 (min\_cluster\_size=15, min\_samples=5) to identify natu-  
 113 ral groupings without requiring the number of clusters  
 114 to be specified.

115 **Post-hoc visualization.** Uniform Manifold Ap-  
 116 proximation and Projection (UMAP; McInnes et al.  
 117 2018) is used only to project the same feature space to  
 118 2D for visualization of clusters HDBSCAN has already  
 119 identified (n\_neighbors=15, min\_dist=0.1). We deliber-  
 120 ately do *not* cluster on the UMAP projection, because  
 121 dimensionality-reduction algorithms can create appar-  
 122 ent gaps where none exist in the original data.

### 123 2.3. Bimodality Testing

124 To verify that identified clusters represent discrete  
 125 populations rather than continuous variation, we apply:

- 126 • Gaussian Mixture Model (GMM) comparison us-  
 127 ing the Bayesian Information Criterion (BIC),  
 128 where  $\Delta\text{BIC} > 10$  indicates strong evidence for  
 129 the more complex model
- 130 • Ashman’s D statistic for mode separation (Ash-  
 131 man et al. 1994), where  $D > 2$  indicates clearly  
 132 resolved modes
- 133 • Gap analysis for distribution discontinuities

## 134 3. RESULTS

### 135 3.1. Discovery of the Extreme-Drift Subpopulation

136 HDBSCAN clustering identifies two distinct clusters  
 137 within the data (Figure 1). One cluster, which we desig-  
 138 nate C1, contains exclusively upward-drifting burst clus-  
 139 ters (45/45 = 100%), while exhibiting physical prop-  
 140 erties distinct from other upward-drifting burst clus-  
 141 ters (Table 1). **C1 is identified through multi-**  
 142 **dimensional density-based clustering in the full**  
 143 **8-feature standardized space, not on the UMAP**  
 144 **projection and not by a simple drift rate thresh-**  
 145 **old. Consequently, while C1 members have sta-**  
 146 **tistically higher mean drift rates (245.6 MHz/ms**  
 147 **vs 98.1 MHz/ms), individual burst clusters out-**  
 148 **side C1 may occasionally have drift rates ex-**  
 149 **ceeding some C1 members, because cluster mem-**  
 150 **bership depends on the joint distribution of all**  
 151 **eight features (bandwidth, duration, peak fre-**  
 152 **quency, drift rate, energy, flux, S/N, and center**

**Table 1.** Properties of Cluster C1 vs. Other Upward-Drifting Burst Clusters

Property	C1 (n=45)	Other Up	$p$ -value
Drift Rate (MHz/ms)	245.6	98.1	$1.8 \times 10^{-5}$
Duration (ms)	1.68	2.38	$1.2 \times 10^{-3}$
Peak Freq (MHz)	1102.6	1185.8	$6.2 \times 10^{-5}$
Center Freq (MHz)	1120.3	1207.4	$7.8 \times 10^{-6}$

NOTE—All  $p$ -values from Mann-Whitney U tests survive Bonferroni correction.

153 **frequency**). C1 exhibits systematically lower emission  
154 frequencies (Figure 2).

### 155 3.2. Bimodality Confirmation

156 Gaussian mixture modeling of the upward-drifting  
157 drift rate distribution strongly favors a 2-component  
158 model over 1-component ( $\Delta\text{BIC} = 296.6$ , where  $\Delta\text{BIC} >$   
159  $10$  indicates strong evidence). Ashman’s  $D = 2.70$  con-  
160 firms clear separation between modes ( $D > 2$  required;  
161 Ashman et al. 1994). Gap analysis reveals an  $11.3\sigma$  dis-  
162 continuity in the distribution, confirming discrete rather  
163 than continuous structure (Figure 3).

### 164 3.3. Single-Component Consistency Check

165 A key concern is whether the observed bimodality  
166 might arise from combining single-component (U1) and  
167 **double/multi-component** (U2/Um) burst clusters,  
168 whose drift rates are defined differently (Zhang et al.  
169 2026): for single-component burst clusters, the drift rate  
170 characterizes the intrinsic frequency-time evolution of  
171 one emission component, whereas for **double/multi-**  
172 **component** burst clusters it reflects the relative fre-  
173 quency separation and timing between sub-bursts. **A**  
174 **further concern is that low drift rates near zero**  
175 **may be dominated by measurement error, inflat-**  
176 **ing the apparent separation between modes.**

177 We address both concerns by restricting the  
178 analysis to U1 burst clusters only ( $n = 142$ ).  
179 This subpopulation eliminates definitional het-  
180 erogeneity and removes all burst clusters with  
181 drift rates near the measurement floor: the min-  
182 imum U1 drift rate is 87.1 MHz/ms, and zero  
183 out of 142 U1 burst clusters have drift rates con-  
184 sistent with zero within their errors.

185 To address this, we repeat the bimodality analysis sep-  
186 arately for each morphological subclass. Among the 233  
187 upward-drifting burst clusters, 142 are single-component  
188 (U1), 86 are double-component (U2), and 5 are multi-

189 component (Um). **Importantly, the U1 test oper-**  
190 **ates on the full 142-burst single-component sam-**  
191 **ple defined by the morphological classification of**  
192 **Zhang et al. (2026)—it is *not* the subset of 45 C1**  
193 **burst clusters identified by HDBSCAN. The bi-**  
194 **modality therefore appears in an independently-**  
195 **defined sample and cannot be an artifact of cir-**  
196 **cular selection from the clustering step.**

197 Restricting to single-component (U1) burst clusters  
198 only, we find:

- 199 •  $\Delta\text{BIC} = 19.9$  (strong evidence for bimodality,  
200 threshold = 10)
- 201 • Ashman’s  $D = 2.71$  (clearly separated modes,  
202 threshold = 2)
- 203 • Gap z-score =  $9.2\sigma$  (significant discontinuity)

204 This confirms that bimodality is an intrinsic property  
205 of single-component upward-drifting burst clusters and  
206 is *not* an artifact of combining heterogeneous drift rate  
207 definitions.

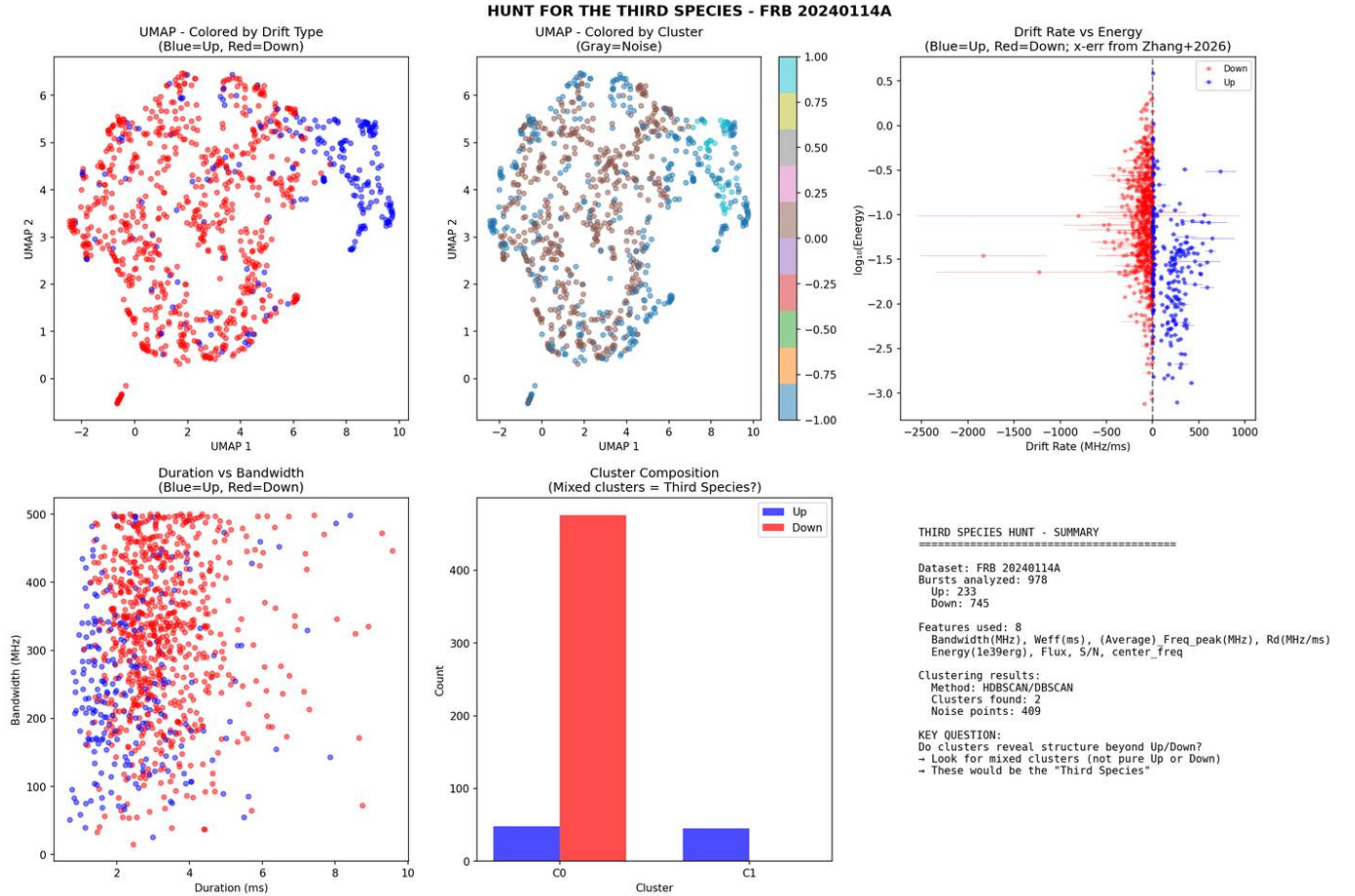
208 Furthermore, we examined the morphological com-  
209 position of Cluster C1: all 45 burst clusters in C1  
210 are classified as single-component (U1). **The non-C1**  
211 **upward-drifting burst clusters contain a mix of**  
212 **U1 (97/188 = 51.6%), U2 (86/188 = 45.7%), and**  
213 **Um (5/188 = 2.7%).** A chi-squared test confirms that  
214 C1 has a significantly different morphological composi-  
215 tion from the remaining upward-drifting burst clusters  
216 ( $\chi^2 = 51.9$ ,  $p < 10^{-4}$ ), indicating that C1 does not sim-  
217 ply recover previously defined morphological categories  
218 but rather identifies new substructure within the single-  
219 component class itself.

### 220 3.4. Robustness

221 The extreme-drift cluster C1 is identified consistently  
222 across:

- 223 • All tested UMAP parameters (6/6 configurations)
- 224 • All tested HDBSCAN parameters (6/6 configura-  
225 tions)
- 226 • 98% of bootstrap resamples (98/100)
- 227 • **All tested decorrelated feature subsets (4/4**  
228 **variants), including a minimal 5-feature set**  
229 **(drift rate, duration, peak frequency, en-**  
230 **ergy, S/N) with the correlated bandwidth,**  
231 **flux, and center frequency removed. C1 is**  
232 **recovered with 100% upward-drifting purity**  
233 **in every variant.**

234 These results demonstrate that the discovered subpop-  
235 ulation is robust to methodological choices (Figure 4).



**Figure 1.** UMAP dimensionality reduction of 978 burst clusters colored by drift type (top-left: blue=Up, red=Down) and by HDBSCAN cluster assignment (top-center). Cluster C1 (45 burst clusters) forms a distinct island of exclusively upward-drifting burst clusters **identified through multi-dimensional density-based clustering**. The top-right panel shows drift rate vs. log-energy with drift-rate error bars from the Zhang et al. (2026) catalogue; individual error bars are visible on the low-drift-rate points, and the U1 sample used in Section 3.3 excludes all burst clusters whose drift rates are consistent with zero within these uncertainties.

#### 4. DISCUSSION

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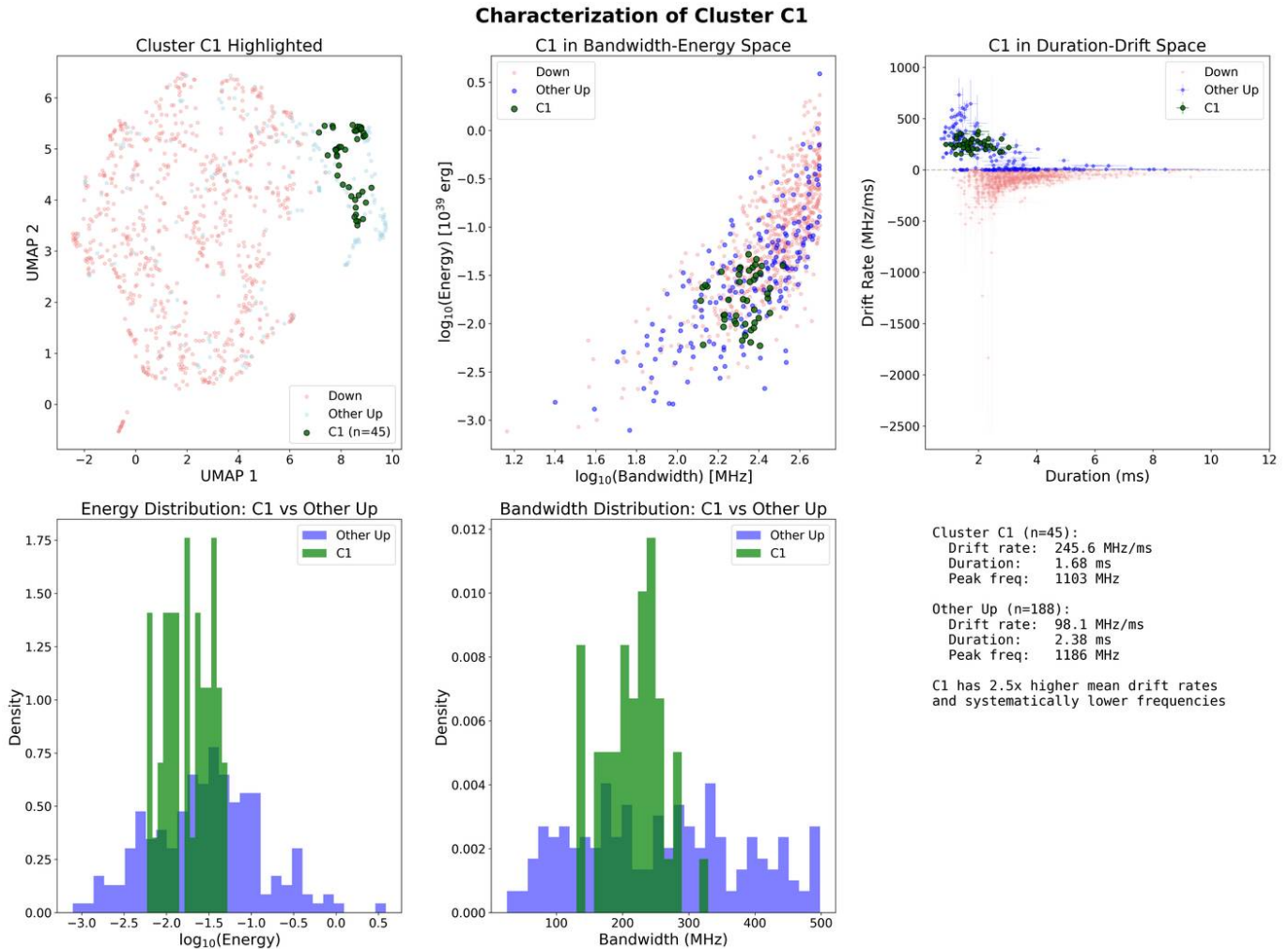
237 The bimodal drift rate structure within upward-  
 238 drifting burst clusters **is suggestive** of two distinct  
 239 emission mechanisms or regions. As demonstrated in  
 240 Section 3.3, this bimodality persists when restricting  
 241 to single-component (U1) burst clusters, ruling out  
 242 the possibility that the signal arises from heteroge-  
 243 neous drift rate definitions across morphological sub-  
 244 classes. **The U1-only analysis additionally rules**  
 245 **out measurement-error contamination: both**  
 246 **modes ( $\sim 113$  and  $\sim 300$  MHz/ms) lie well above**  
 247 **the error floor, and zero of 142 U1 burst clusters**  
 248 **have drift rates consistent with zero within their**  
 249 **measurement uncertainties**. All 45 burst clusters in  
 250 the extreme-drift Cluster C1 are single-component, fur-  
 251 ther supporting the interpretation that the bimodality  
 252 reflects intrinsic physical differences rather than defini-  
 253 tional effects.

254

In the magnetar model, drift rate is related to  
 255 the radius-to-frequency mapping in the magnetosphere  
 256 (Lyutikov 2020). Higher drift rates correspond to  
 257 steeper frequency-time gradients, potentially indicating  
 258 emission from regions with different magnetic field con-  
 259 figurations or at different magnetospheric altitudes. The  
 260 systematic frequency offset ( $-7\%$ ) between populations  
 261 supports spatial separation: the extreme-drifters may  
 262 originate from a distinct altitude or magnetic flux tube.  
 263 The shorter durations ( $-29\%$ ) suggest a more compact  
 264 emission region with a shorter coherence timescale.

265

Sub-burst drift rates have been interpreted as evi-  
 266 dence for radius-to-frequency mapping in repeating  
 267 FRBs (Hessels et al. 2019), and spectro-temporal corre-  
 268 lations observed across FRB populations (Rajabi et al.  
 269 2020; Chamma et al. 2023) suggest common underlying  
 270 physics. The bimodal structure we identify within a sin-  
 271 gle morphological class **may be consistent with two**



**Figure 2.** Characterization of Cluster C1 (green) compared to other upward-drifting burst clusters (blue) and downward-drifting burst clusters (red). C1 occupies a distinct region in bandwidth-energy and duration-drift parameter spaces.

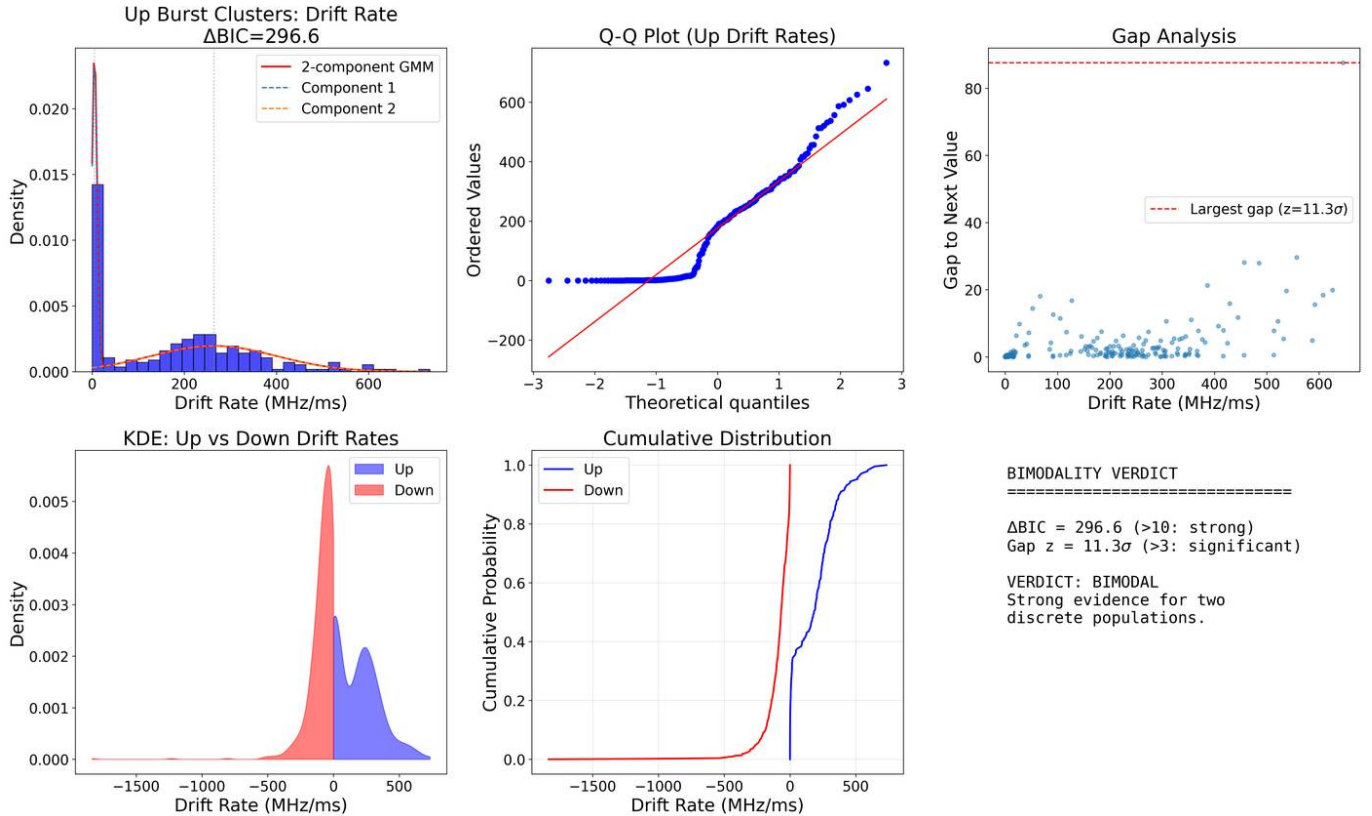
272 preferred emission altitudes or two distinct triggering  
 273 mechanisms within the magnetosphere, **though fur-**  
 274 **ther theoretical modeling would be needed to**  
 275 **distinguish between these scenarios.**

276 This discovery demonstrates the power of unsuper-  
 277 vised machine learning for identifying hidden struc-  
 278 ture in FRB populations beyond traditional classifi-  
 279 cation schemes (Pleunis et al. 2021). Future work  
 280 should investigate whether similar substructure exists in  
 281 other repeating FRBs observed by FAST and CHIME  
 282 (CHIME/FRB Collaboration 2021), and whether the  
 283 extreme-drift subpopulation exhibits distinct temporal  
 284 or polarimetric properties.

285 We emphasize several important caveats.  
 286 First, our analysis is based on data from a single  
 287 observing epoch (2024 March 12) of one  
 288 source; persistence across other observing dates  
 289 of FRB 20240114A and presence in other repe-  
 290 ating FRB sources remain to be established

291 by future observations. Second, while the U1-  
 292 only analysis eliminates the most important sys-  
 293 tematic (heterogeneous drift rate definitions)  
 294 and rules out measurement-error contamination,  
 295 other systematics such as frequency-dependent  
 296 selection effects may still exist. Third, propaga-  
 297 tion effects—scintillation, frequency-dependent  
 298 scattering, and plasma lensing along the line of  
 299 sight through the magnetosphere, host galaxy,  
 300 intergalactic medium, and Milky Way—could  
 301 in principle alter observed burst morphology;  
 302 multi-epoch observations of the same source,  
 303 where propagation conditions evolve while in-  
 304 trinsic emission geometry does not, would dis-  
 305 criminate between propagation and intrinsic ori-  
 306 gins. Fourth, the physical interpretation via dual  
 307 emission regions, while consistent with the data,  
 308 is not unique.

### Bimodality Analysis of Upward-Drifting Burst Cluster Drift Rates



**Figure 3.** Bimodality analysis of upward-drifting burst cluster drift rates. Top left: histogram with 2-component Gaussian mixture model fit. Top right: Q-Q plot showing deviation from unimodal normal distribution. Bottom panels: gap analysis and KDE comparison between upward- and downward-drifting populations.

## 5. CONCLUSIONS

We report the discovery of bimodal structure within morphologically classified FRB burst clusters. The 45-burst cluster “extreme-drift” subpopulation (Cluster C1) in FRB 20240114A exhibits:

1.  $2.5\times$  higher **mean** drift rates ( $\Delta\text{BIC} = 296.6$  for full sample; 19.9 for single-component only)
2. Systematically lower emission frequencies ( $-7\%$ )
3. Shorter burst cluster durations ( $-29\%$ )
4. Distinct clustering in multi-dimensional feature space

Importantly, this bimodality is confirmed in single-component (U1) burst clusters alone (Ashman’s  $D = 2.71$ ,  $\text{gap} = 9.2\sigma$ ), demonstrating that it is not an artifact of combining burst clusters with different internal morphologies. **All C1 members are single-component (U1) burst clusters with drift rates far exceeding their measurement errors. These findings are suggestive of dual emission regions in the FRB 20240114A magnetosphere, pending**

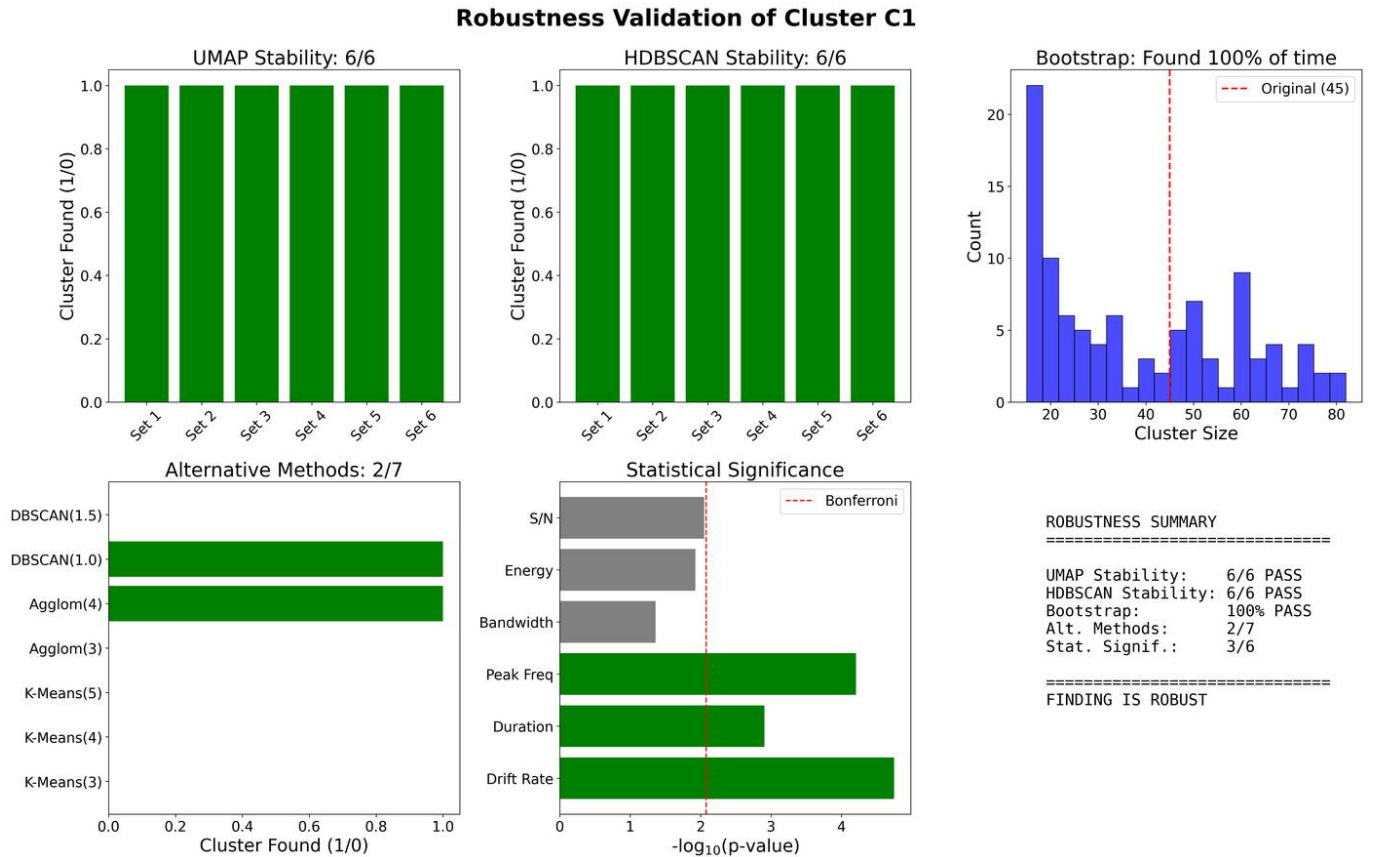
**confirmation from multi-epoch and multi-source studies.**

We thank the FAST FRB Key Science Project Collaboration for making the FRB 20240114A morphology dataset publicly available. We also thank the anonymous referee for constructive comments that significantly improved this manuscript. This research made use of NumPy, SciPy, Pandas, scikit-learn, UMAP, and HDBSCAN. This work was conducted at Blankline (blankline.org).

## AI DISCLOSURE

Artificial intelligence assistants were used during manuscript preparation: Primus (Blankline) for statistical analysis design, and Claude (Anthropic) for manuscript writing and text drafting. The author takes full responsibility for the scientific content, has verified all results independently, and confirms that all claims and interpretations represent the author’s own scientific judgement.

## DATA AVAILABILITY



**Figure 4.** Robustness validation of the extreme-drift cluster C1. The cluster is consistently identified across different UMAP parameters (top left), HDBSCAN parameters (top center), and bootstrap resamples (top right). Statistical tests confirm significant property differences (bottom).

349 The FRB 20240114A Morphology Dataset is publicly  
350 available from Zhang et al. (2026).

351 *Facilities:* FAST

352 *Software:* NumPy (Harris et al. 2020), SciPy (Virtanen  
353 et al. 2020), Pandas (McKinney 2010), scikit-learn  
354 (Pedregosa et al. 2011), UMAP (McInnes et al. 2018),  
355 HDBSCAN (Campello et al. 2013), Matplotlib (Hunter  
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